

# Automatically Proving Memory Safety and Termination of C-Programs

Alexander Weinert  
RWTH Aachen University

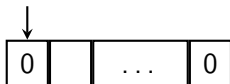
Research Area Computer Science 2  
Published: (Termination with Pointer Arithmetic, Ströder et al., 2014)

Feb 23, 2015

## An Example

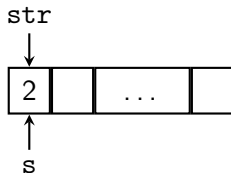
```
int strlen(char* str) {  
    char* s = str;  
    while(*(++s));  
    return s-str;  
}
```

str



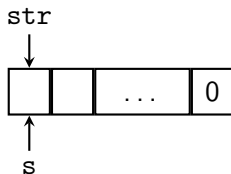
## An Example

```
int strlen(char* str) {  
    char* s = str;  
    while((*s)++);  
    return s-str;  
}
```



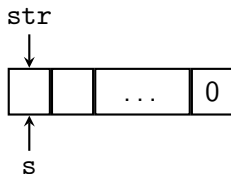
## An Example

```
int strlen(char* str) {  
    char* s = str;  
    while(*(s++));  
    return s-str;  
}
```



## An Example

```
int strlen(char* str) {  
    char* s = str;  
    while(*s) s++;  
    return s-str;  
}
```

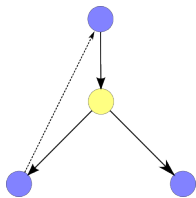
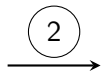


# Big Picture

THE  
**C**  
PROGRAMMING  
LANGUAGE



LLVM

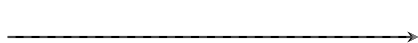


Symbolic Execution Graph

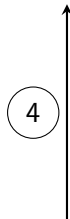


$f(x) \rightarrow g(x + 1)$   
 $g(x) \rightarrow g(x - 1)$

Integer Transition  
System



YES/NO/  
MAYBE

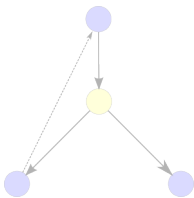


# C to LLVM

THE  
**C**  
PROGRAMMING  
LANGUAGE



LLVM



Symbolic Execution Graph



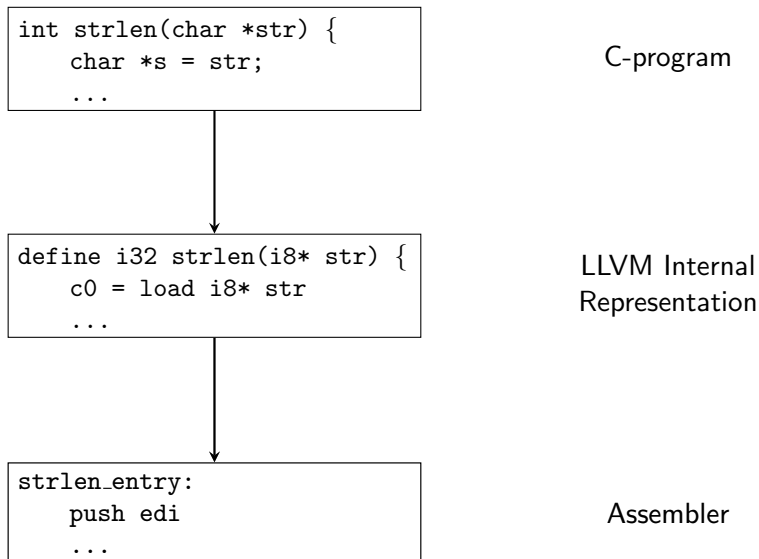
$f(x) \rightarrow g(x + 1)$   
 $g(x) \rightarrow g(x - 1)$

Integer Transition  
System

YES/NO/  
MAYBE



# LLVM Compiler Infrastructure





## Some LLVM Instructions

- ▶ Control Flow Instructions
  - ▶ `ret`, `br`, `call`, ...
- ▶ Arithmetic Instructions
  - ▶ `add`, `icmp`, ...
- ▶ Bitwise Instructions
  - ▶ `shl`, `and`, ...
- ▶ Memory Instructions
  - ▶ `alloca`, `load`, `store`, ...

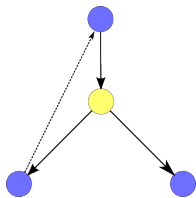
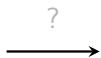
Complete Reference: <http://llvm.org/docs/LangRef.html>

# LLVM to Symbolic Execution Graph

THE  
**C**  
PROGRAMMING  
LANGUAGE



LLVM



Symbolic Execution Graph



YES/NO/  
MAYBE

?

$f(x) \rightarrow g(x + 1)$   
 $g(x) \rightarrow g(x - 1)$

Integer Transition  
System

# Problem Definition

Given: LLVM Program, Entry Point

Goal: Description of *at least all possible runs* from the entry point

Idea: Abstract interpretation of program states

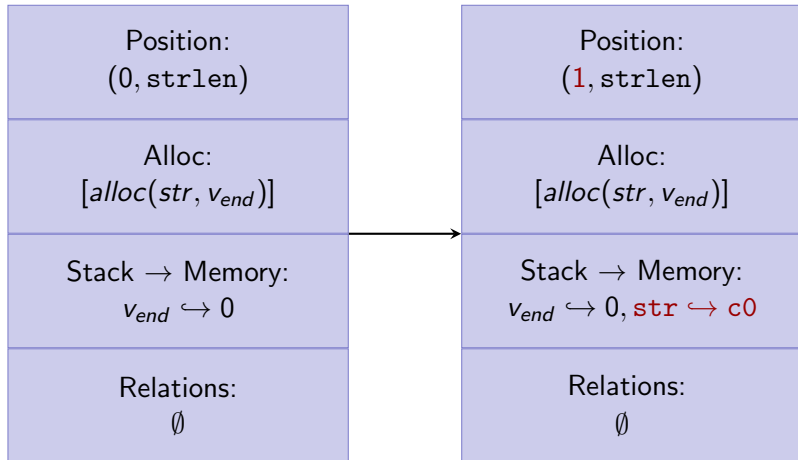
# Abstract States

Position:	$(0, \text{strlen})$
Alloc:	$[\text{alloc}(\text{str}, v_{\text{end}})]$
Stack $\rightarrow$ Memory:	$v_{\text{end}} \hookrightarrow 0$
Relations:	$\emptyset$

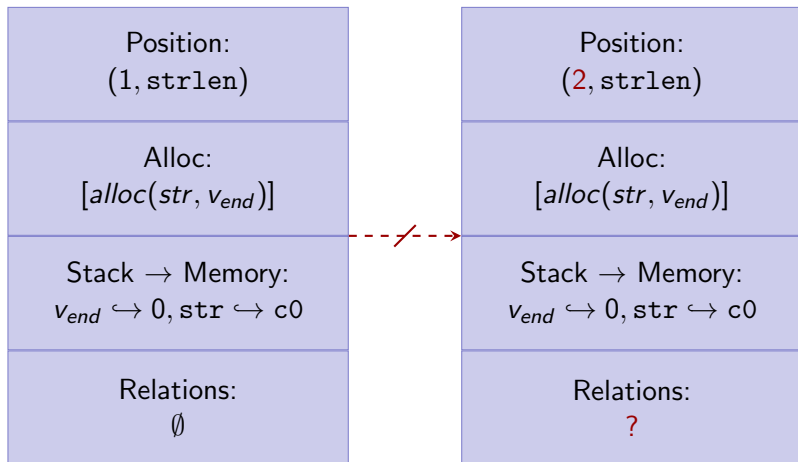
Entry Point:      `define i32 strlen(i8* str) {`  
                      `c0 = load i8* str`  
                      `...`

# Evaluation of Abstract States

```
c0 = load i8* str
```

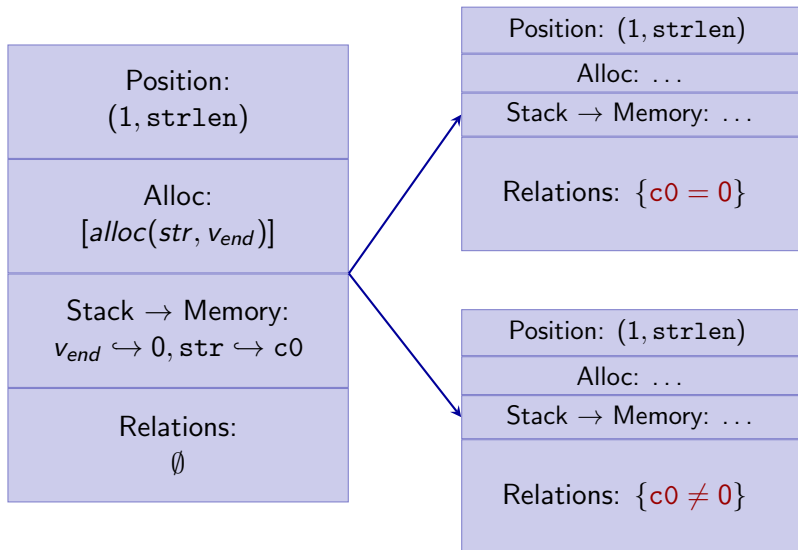


## Refinement of Abstract States

$$c0zero = \underbrace{icmp\ eq\ i8\ c0,\ 0}_{c0==0}$$


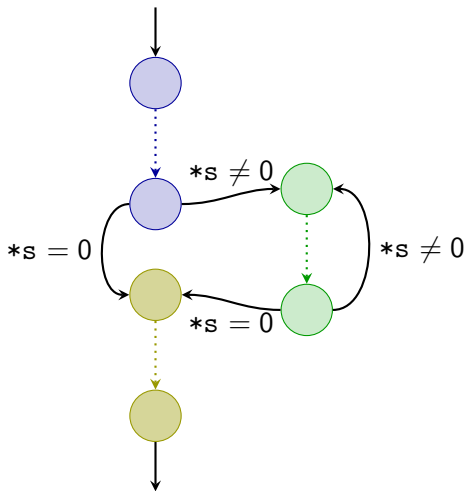
# Refinement of Abstract States

```
c0zero = icmp eq i8 c0, 0
```



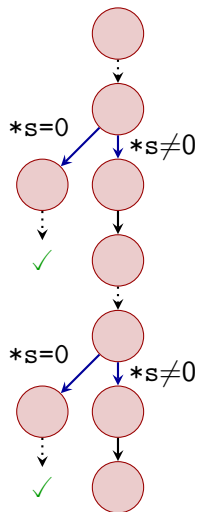
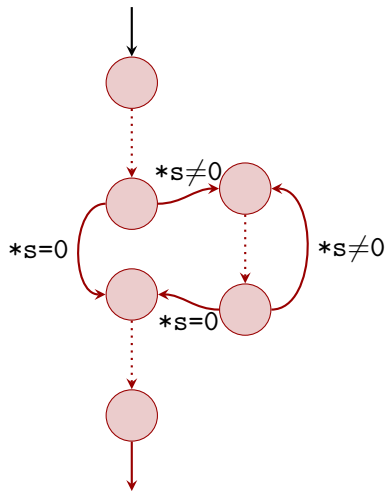
## Merging of Abstract States

```
int strlen(char *str) {  
    char *s = str;  
    while(*s) s++;  
    return s-str;  
}
```

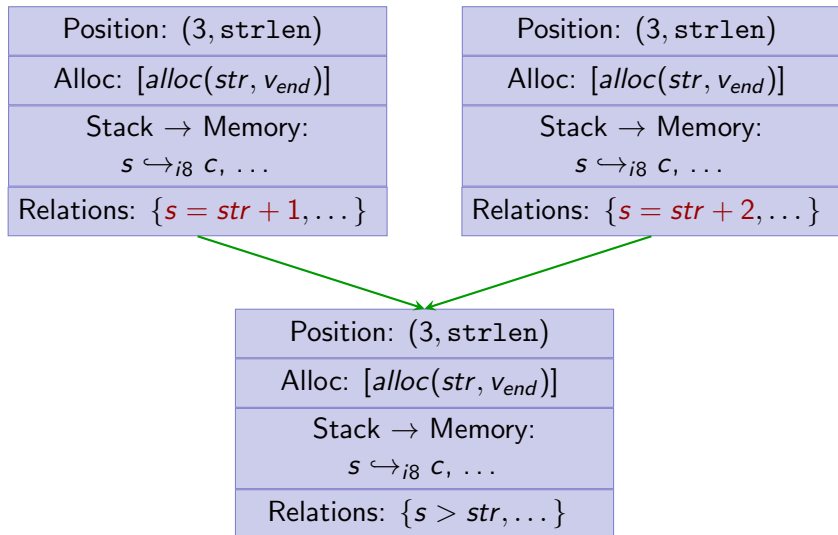




# Merging of Abstract States

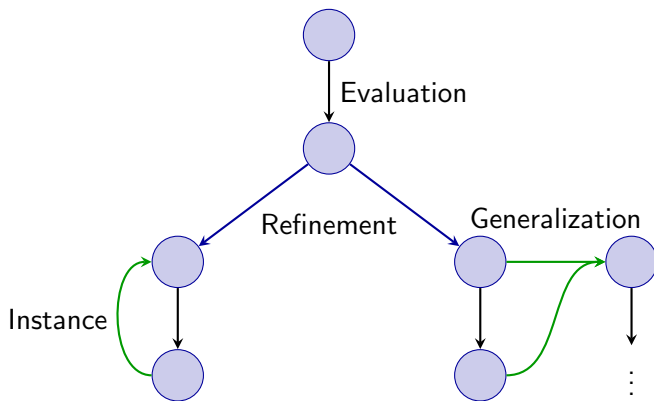


## Merging of Abstract States





## Summary: Symbolic Execution Graphs

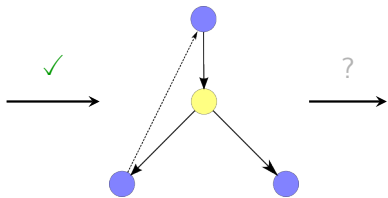


# Symbolic Execution Graph to Integer Transition System

THE  
**C**  
PROGRAMMING  
LANGUAGE



LLVM



Symbolic Execution Graph

YES/NO/  
MAYBE

?

$f(x) \rightarrow g(x + 1)$   
 $g(x) \rightarrow g(x - 1)$

Integer Transition  
System

# Integer Transition Systems

Term Rewriting System:

$$f(x, y) \rightarrow g(y, x)$$

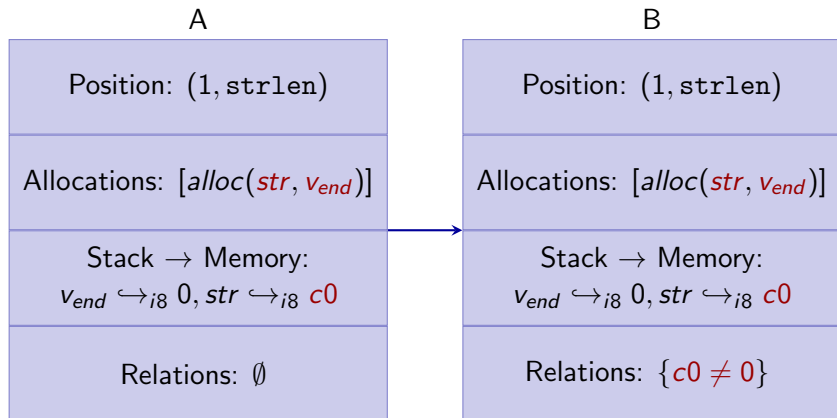
Integer Transition System:

$$f(x, y) \rightarrow g(y + 1, x - 2)$$

Integer Transition System:

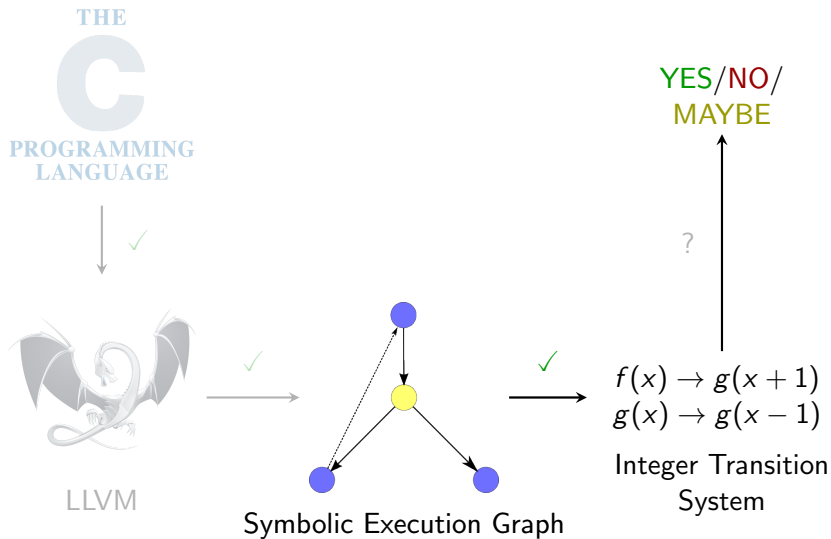
$$f(x, y) \rightarrow g(y + 1, x - 2) \quad | \quad x > 0$$

# Symbolic Execution Graph to Integer Transition System



$$f_A(\text{str}, v_{\text{end}}, c0) \rightarrow f_B(\text{str}, v_{\text{end}}, c0) \mid c0 \neq 0$$

# Termination of Integer Transition System





# Termination of Integer Transition System

Well-studied problem

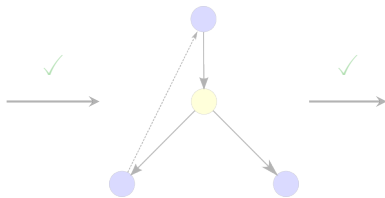
Use known techniques to show termination,  
e.g. (Termination of Integer Term Rewriting, Fuhs et al., 2009)

# Termination of Integer Transition System

THE  
**C**  
PROGRAMMING  
LANGUAGE



LLVM



Symbolic Execution Graph

YES/NO/  
MAYBE



$f(x) \rightarrow g(x + 1)$   
 $g(x) \rightarrow g(x - 1)$

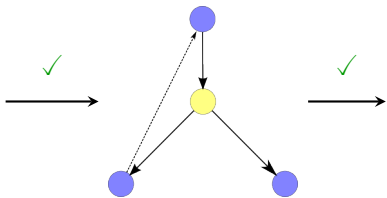
Integer Transition  
System

# Overview

THE  
**C**  
PROGRAMMING  
LANGUAGE



LLVM



Symbolic Execution Graph

YES/NO/  
MAYBE



$f(x) \rightarrow g(x + 1)$   
 $g(x) \rightarrow g(x - 1)$

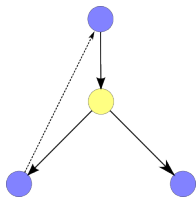
Integer Transition  
System

# My Contributions

THE  
**C**  
PROGRAMMING  
LANGUAGE



LLVM



Symbolic Execution Graph



YES/NO/  
MAYBE



$f(x) \rightarrow g(x + 1)$   
 $g(x) \rightarrow g(x - 1)$

Integer Transition  
System

# My Contributions

Given: Abstract State  $s$ , Integer Relation  $r$

Question: Does  $s \models r$ ?

# My Contributions

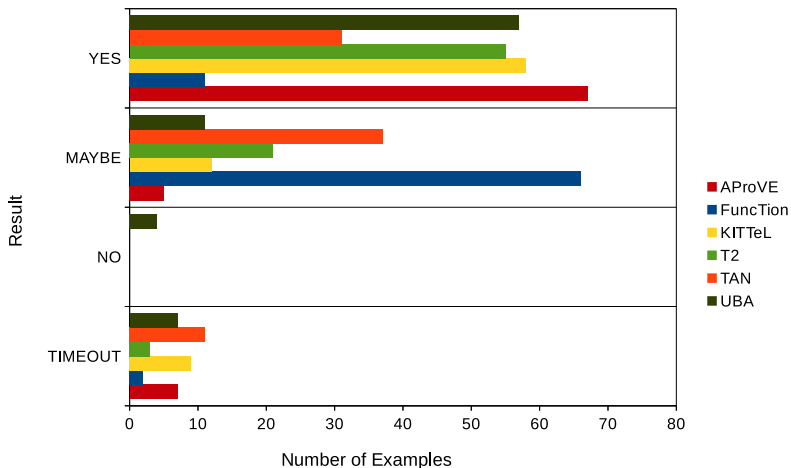
- ▶ Reduction from state to set of arithmetic relations
- ▶ Inference of knowledge from states
  - ▶ Formulation of inference in terms of integer relations
  - ▶ New framework for inference
  - ▶ Parameterization of framework with abstract arithmetic domain
  - ▶ Formulation of existing inference in framework

# My Contributions

- ▶ Use of Octagon Domain for inference of relations
  - ▶ (The Octagon Abstract Domain, Miné, 2006)
- ▶ Experimental comparison
  - ▶ “Traditional” inference
  - ▶ Inference in framework
  - ▶ New inference based on Octagons

# Evaluation: Empirical Evaluation

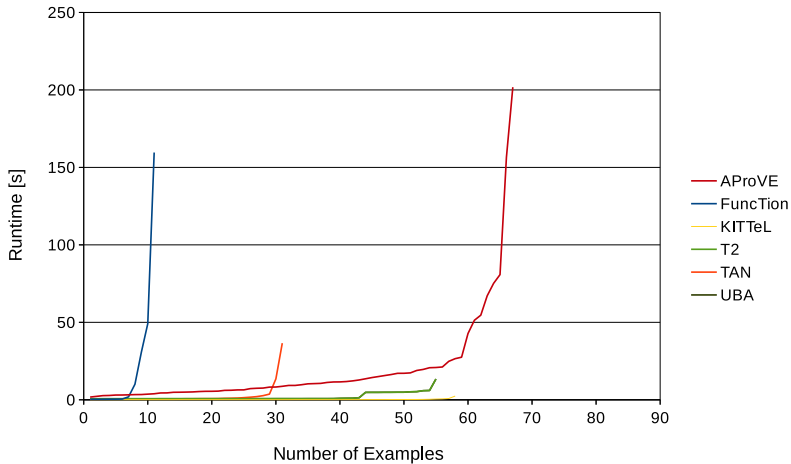
79 Integer Programs, Timeout: 300s





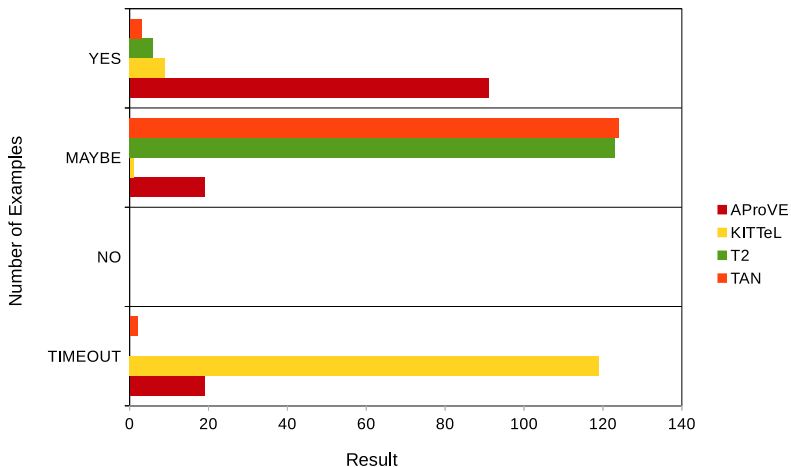
# Evaluation: Empirical Evaluation

79 Integer Programs, Timeout: 300s



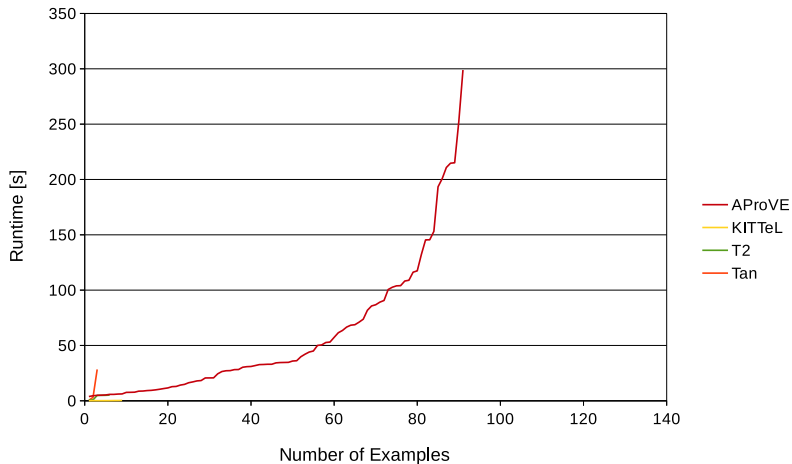
# Evaluation: Empirical Evaluation

129 Pointer Programs, Timeout: 300s



# Evaluation: Empirical Evaluation

129 Pointer Programs, Timeout: 300s



Complete evaluation at  
<http://aprove.informatik.rwth-aachen.de/eval/Pointer/>

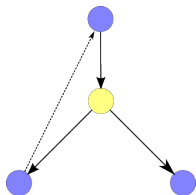
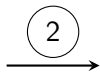
Thank you for your attention

`www.alexanderweinert.net`  
`alexander.weinert@rwth-aachen.de`

THE  
**C**  
PROGRAMMING  
LANGUAGE



LLVM



Symbolic Execution Graph



$f(x) \rightarrow g(x + 1)$   
 $g(x) \rightarrow g(x - 1)$

Integer Transition  
System

YES/NO/  
MAYBE

